

2D Matlab basics

```
clear all, close, clc
set_defaults()
```

In two dimensions we will extensively use two functions for plotting:

1. [meshgrid\(\)](#)
2. [reshape\(\)](#)

These functions have an internal logic that is counter-intuitive and forces us to use certain conventions to avoid trouble later.

Meshgrid()

The function `meshgrid()` takes two vectors **x** and **y** that contain the location of the grid points and generates matrices **X** and **Y** that are used by all 2D Matlab plotting functions, in particular [contour\(\)](#), [contourf\(\)](#) and [surf\(\)](#).

```
f = @(x,y) x.*y;
g = @(x,y) y;
```

```
Nx = 4; Ny = 3; N = Nx*Ny
```

```
N = 12
```

```
x = linspace(0,1,Nx)
```

```
x = 1x4
      0    0.3333    0.6667    1.0000
```

```
y = linspace(0,2,Ny)
```

```
y = 1x3
      0     1     2
```

```
[X,Y] = meshgrid(x,y)
```

```
X = 3x4
      0    0.3333    0.6667    1.0000
      0    0.3333    0.6667    1.0000
      0    0.3333    0.6667    1.0000
```

```
Y = 3x4
      0     0     0     0
      1     1     1     1
      2     2     2     2
```

```
size(X)
```

```
ans = 1x2
      3     4
```

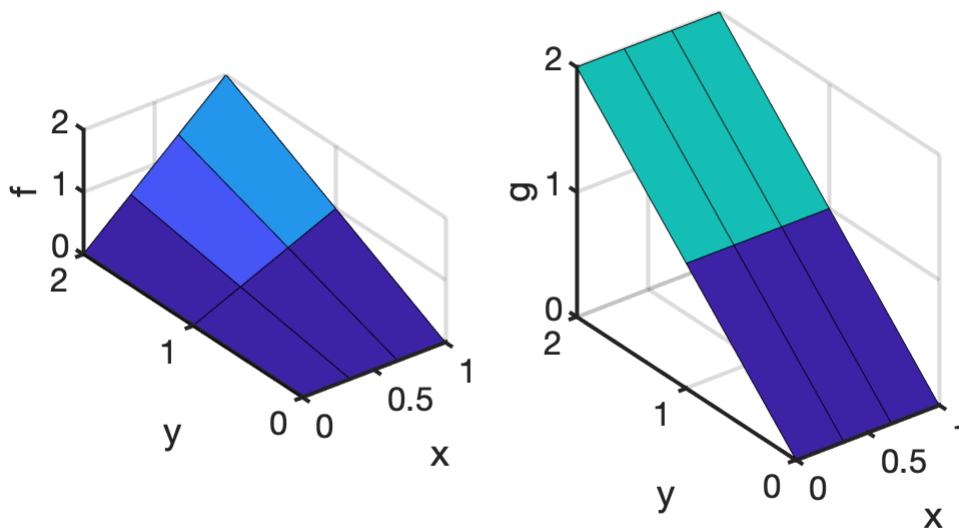
In the matrices **X** and **Y**, the *y*-value increases with the row index, *i*, and the *x*-value increases with the column index, *j*. Since we index matrices as **X**(*i*,*j*) and **Y**(*i*,*j*), the first index is the *y*-coordinate. **This makes it natural to order our grid *y*-first - see below!**

```

subplot 121
surf(X,Y,f(X,Y))
xlabel 'x', ylabel 'y', zlabel 'f'
pbaspect([1 2 .8])

subplot 122
surf(X,Y,g(X,Y))
xlabel 'x', ylabel 'y', zlabel 'g'
pbaspect([1 2 2*.8])

```



Reshape()

The solution of the PDE is calculated as a column vector, \mathbf{u} . To plot the solution \mathbf{u} has to be reshaped into a matrix that is compatible with the ordering of the \mathbf{X} and \mathbf{Y} matrices produced by meshgrid. The Matlab function `reshape()` allows us to move from vectors to matrices and back.

1) From a matrix to a vector

There are two options to turn a matrix into a column vector.

1. Colon operator
2. `reshape()`

```
x
```

```
x = 3x4
```

```

0    0.3333    0.6667    1.0000
0    0.3333    0.6667    1.0000
0    0.3333    0.6667    1.0000

```

```
x1 = X(:)
```

```

x1 = 12x1
     0
     0
     0
 0.3333
 0.3333
 0.3333
 0.6667
 0.6667
 0.6667
 1.0000
     ⋮

```

```
x2 = reshape(X,N,1)
```

```

x2 = 12x1
     0
     0
     0
 0.3333
 0.3333
 0.3333
 0.6667
 0.6667
 0.6667
 1.0000
     ⋮

```

Note, both ways stack the columns of \mathbf{X} into a column.

Of course reshape() is the more general, it allows you to transform \mathbf{X} into any matrix or vector with the same number of elements

```
reshape(X,1,N)    % row vector
```

```

ans = 1x12
     0         0         0    0.3333    0.3333    0.3333    0.6667    0.6667 ...

```

```
reshape(X,Nx,Ny) % flip the dimension of the matrix
```

```

ans = 4x3
     0    0.3333    0.6667
     0    0.3333    1.0000
     0    0.6667    1.0000
 0.3333    0.6667    1.0000

```

1) From vector to matrix

Suppose the solution is given by $\mathbf{g} = g(\mathbf{x})$

```
soln = g(X(:),Y(:))
```

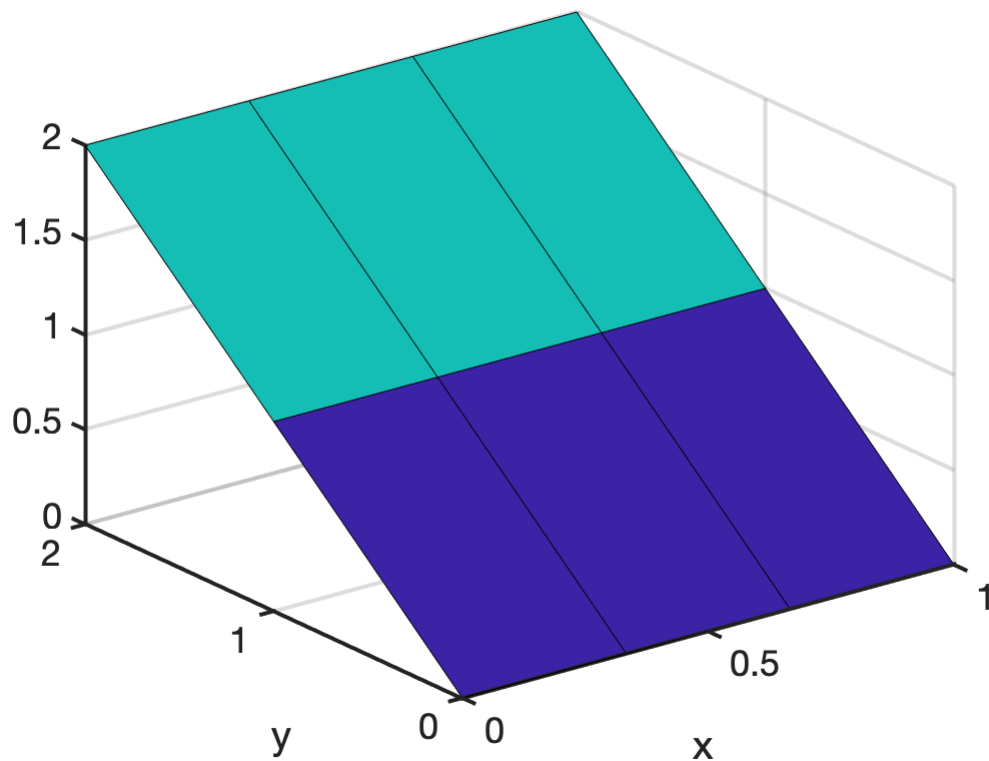
```
soln = 12x1
 0
 1
 2
 0
 1
 2
 0
 1
 2
 0
 ⋮
 ⋮
```

To plot this solution we need to transfer it back to a matrix. To be compatible with X and Y from meshgrid this matrix has to be of size N_y by N_x !

```
SOLN = reshape(soln,Ny,Nx)
```

```
SOLN = 3x4
 0  0  0  0
 1  1  1  1
 2  2  2  2
```

```
figure
surf(X,Y,SOLN)
xlabel('x'), ylabel('y')
```



Notice, that N_y is the first entry, because `meshgrid()` has a y-first ordering!

2D grid with y-first ordering

Given that `meshgrid()` has an internal y-first ordering, we use a computational grid with a y-first ordering. This way we avoid a lot of problems!

```
Nx = 4;
Ny = 3;
N = Nx*Ny;

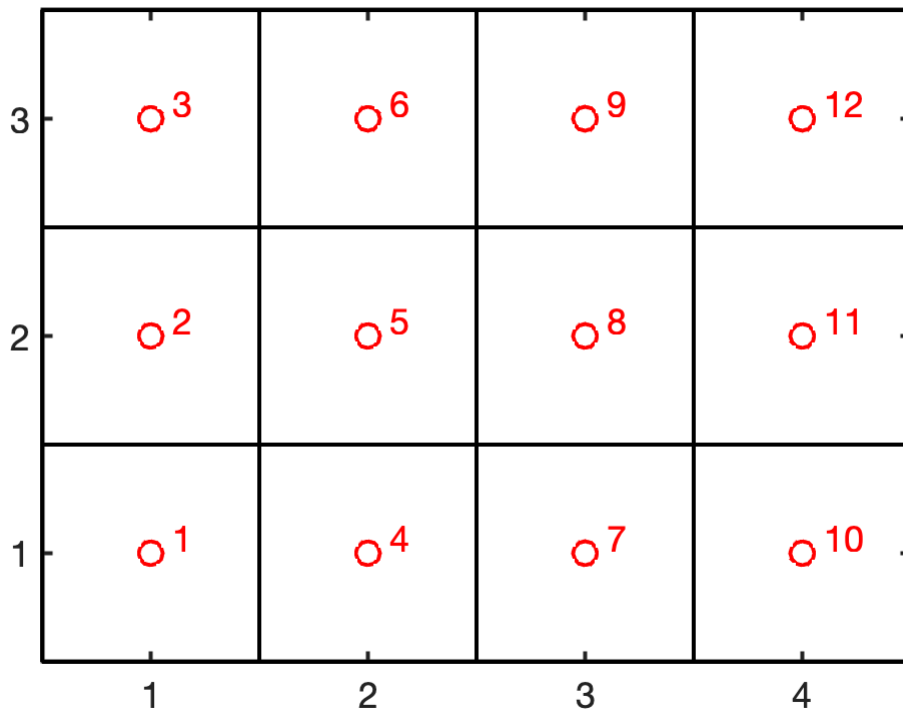
x = 1:Nx;
y = 1:Ny;
dof = 1:N;

[X,Y] = meshgrid(x,y);

DOF = reshape(dof,Ny,Nx)
```

```
DOF = 3x4
     1     4     7    10
     2     5     8    11
     3     6     9    12
```

```
plot([.5 Nx+.5 Nx+.5 .5 .5],[.5 .5 Ny+.5 Ny+.5 .5],'k'), hold on
for i=1:Nx
    plot([x(i)+.5 x(i)+.5],[.5 Ny+.5],'k-')
    for j=1:Ny
        plot([.5 Nx+.5],[y(j)+.5 y(j)+.5],'k-')
        plot(X(j,i),Y(j,i),'ro','markerfacecolor','w')
        text(X(j,i)+.1,Y(j,i)+.07,num2str(DOF(j,i)),'fontsize',18,'color','r')
    end
end
set(gca,'xtick',[1:Nx],'ytick',[1:Ny])
axis equal tight
```



Tensor Product

Because we are discretizing the differential operators on a regular mesh the tensor product will be a key for the efficient, clean and simple implementation of the multi dimensional operators. The tensor product is also called the Kronecker product, hence the respective Matlab function is `kron()`. We will learn more about it later, but below is the basic use.

```
A = eye(4);
B = [1 2; ...
     4 5];

AoB = kron(A,B)

BoA = kron(B,A)
```

Auxillary functions

set_defaults()

```
function [] = set_defaults()
set(0, ...
    'defaultaxesfontsize', 18, ...
    'defaultaxeslinewidth', 2.0, ...
```

```
'defaultlinewidth', 2.0, ...  
'defaultpatchlinewidth', 2.0, ...  
'DefaultLineMarkerSize', 12.0);  
end
```